

A Feature Extraction and Machine Learning Based Approach for Glaucoma Detection from Fundus Images

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Abstract: A chronic eye condition known as glaucoma causes progressive damage to the optic nerve and astrocytes as a result of excessive intraocular pressure (IOP). It is the second leading global contributor to vision loss and blindness. Stopping the disease's progression towards total eyesight loss depends on early diagnosis. The diagnosis of glaucoma strongly depends on the expertise of a glaucoma expert ophthalmologist due to the complicated and varied disease pathology. To protect a patient's eyesight, it is critical to identify glaucoma in its early stages. The ability to design algorithms that can automatically and accurately identify glaucoma from fundus images has been made possible by recent advancements in image processing and related machine learning techniques. This work presents a fundus image enhancement, segmentation, and denoising approach. Additional statistical measurements of the image have been made that might aid in the identification of glaucoma. When compared to current techniques, the suggested approach performs better than baseline procedures in terms of classification accuracy.

Keywords: *Glaucoma Detection, Fundus Image Processing, Discrete Wavelet transform, Feature Extraction., ANN, Classification Accuracy*

INTRODUCTION

Glaucoma is also referred to as the silent snatcher of sight, and is the leading reason causing irreversible blindness worldwide. The risk factors and severity of sub-types of the disease may vary among races of different countries ^[1]. It has been found that glaucoma accounts for around 3 million cases of complete blindness and approximately 4 million cases resulting in visual impairment worldwide ^[2]. It is apprehended that the number of people affected by any sub-type of glaucoma will exceed a staggering 110 million by 2040 ^[3]. Although glaucoma can be found to affect people irrespective of their age, however higher chances of occurrence (in between 1%-4%) is found among patients over the age of 40 ^[4]. The fundamental reason for the onset of glaucoma is the elevated level of intraocular pressure (IOP). Increased levels of IOP adversely affects the optic nerve causing irreversible damage, resulting in loss or impairment in vision depending on the magnitude of damage ^[5]. To save the vision of the individuals affected by glaucoma, the fundamental mechanism is to clinically reduce the levels of IOP. Clinical monotherapy or combination therapy, and in some cases surgical intervention may be required to reduce the levels of IOP to normal values ^[6]. While conventional medical practices have

been prevalent in the diagnosis and subsequent treatment of glaucoma, recent advancements in the domain of artificial intelligence and machine learning have opened up new avenues for the early and accurate detection of glaucoma ^[7]. Automated computational tools can aid ophthalmologists to detect glaucoma at relatively early stages so as to minimize the damage to optic nerve and hence reduce visual impairments. Moreover, it would form the basis for a strong second opinion. It can be particularly useful in areas which lack advanced medical facilities, typically common in remote areas of low income group countries ^[8]. Several automated techniques have been developed and explored based on the statistical analysis of the fundus image. The basic approach is to pre-process the image to remove the effects of noise and disturbance followed by feature extraction and classification using a machine learning based classifier ^[10]. The machine learning based classifier is trained with images of two categories viz. affected by glaucoma and unaffected with glaucoma. The classifier tries to identify the patterns in the data and hence classify any new sample of the fundus image as glaucoma positive or negative ^[11].

A typical illustration of glaucoma negative and glaucoma positive fundus images along with the fundus camera are illustrated in figure 1 ^[12].

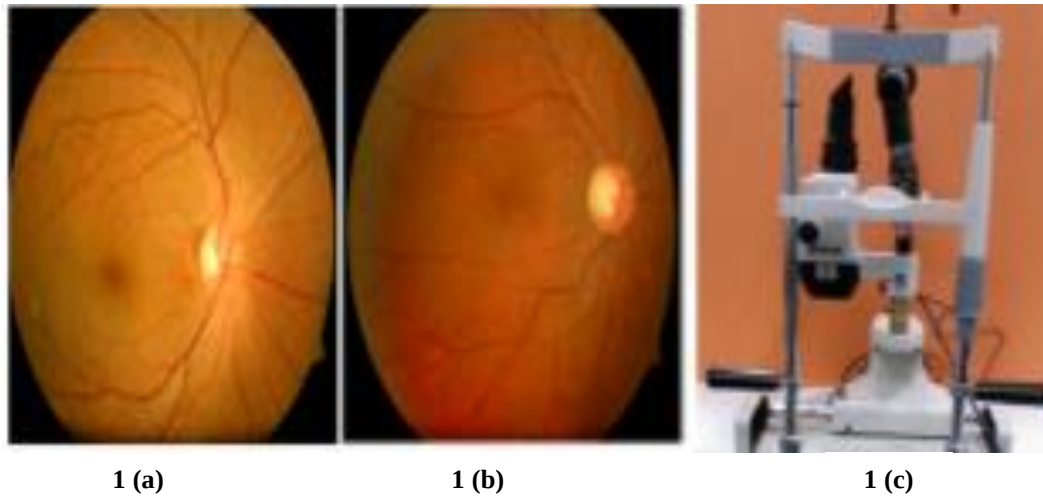


Fig. 1. (a) Healthy (b) Glaucoma (c) Fundus Camera

The fundus images obtained from fundus imaging need to be processed and analysed to extract critical features for the decision on presence or absence of glaucoma or pre-glaucoma like symptoms [13]. Due to the occurrence of noise and disturbance effects while capturing, retrieving, processing and storing the images, the final classification may be prone to errors [14]. This necessitates case sensitive noise removal and image restoration techniques which can enhance the quality of the images under interest so as to facilitate feature extraction and pattern recognition [15]. This paper presents an combined approach for image enhancement and feature extraction pertaining to fundus images which would facilitate automated detection of glaucoma.

MATERIALS AND METHODS

With the availability of exhaustive digital data records in the medical field coupled with the increasing processing powers of computational algorithms, automated detection of glaucoma has gained prominence. For accurate classification of glaucoma images, it is fundamentally important to pre-process the images prior to actual classification. In this paper, each of the sub-processes employed for image enhancement and subsequent feature extraction are explained in this section.

RGB to Grayscale Conversion: Typically, acquired fundus images are contain three color channels which are Red, Green and Blue (RGB channels). Analyzing high resolution RGB images requires much higher compute power as compared to analyzing images with a single intensity variable as in the case of grayscale images (with grayscale or intensity variable). The luminosity algorithm for RGB to grayscale conversion is done based on the following relation [16]:

$$I_{GS} = 0.28R + 0.5G + 0.09B \quad (1)$$

Here,

I_{GS} corresponds the pixel value of the grayscale image.
 R corresponds to the red component of the pixel.
 G corresponds to the green component of the pixel.
 B corresponds to the blue component of the pixel.

The benefit of the approach is the conversion of the image dataset from three channels to one channel reducing the complexity of the approach.

Illumination Correction: Illumination correction corresponds to the removing the inherent illumination inconsistencies of the image due to poor or inadequate lighting conditions, variations in the reflections from the target surface due to inherent heterogeneity, variations in the angle of capture, slight movements in the position and/or orientation of the source, variations in the wavelength (monochromatic nature) of the source and inconsistencies in the characteristics of the sensing device [17]. In this approach, a Gaussian Kernel Function is used for illumination correction as it is effective in normalizing the dynamic range of the image intensities, and is mathematically expressed as:

$$G(x, y) = ke^{\frac{-(x^2+y^2)}{s^2}} \quad (2)$$

Here,

$G(x, y)$ is the Gaussian Kernel.

k represents the normalizing co-efficient.

s represents the scaling co-efficient of the kernel.

(x, y) represent the spatial co-ordinates.

The reflection co-efficient value $I_R(x, y)$ is estimated by convolving the input image and the Gaussian function in the periphery bound the contour 'C'. The weight co-efficient w is updated throughout the contour for the number of scales $i =$

1: n . Further a linear transform to adjust the objectively captured image I and the corrected image I_c is given by:

$$I_c = \beta_1 \log_e I + \beta_2 \quad (3)$$

Here,

I and I_c corresponds to the physically captured and illumination corrected images respectively.

β_1 and β_2 are correction constants.

The next process is the computation of the two-dimensional spatial correlation given by:

$$C(x, y) = \frac{I(x, y) - I_c(x, y)}{I(x, y) - I_B(x, y)} \cdot k \quad (3)$$

Here,

C represents the correlation.

k denotes the normalizing co-efficient.

I denotes the original image

I_c denotes image correlation

I_B denotes image background

The histogram normalization is computed based on the difference in the eigen values of the original and corrected image given by:

$$|kI - I_c| \quad (4)$$

The covariance of the image can be computed as:

$$C_V = \frac{\text{mean}[I(x, y) - I_c(x, y)]}{|kI - I_c|} \quad (5)$$

Here,

mean denotes the average operation.

The subsequent process is to add the product of the weight matrix and normalized co-variance co-efficient to the originally corrected image given by:

$$N_I = I(x, y) - I_c\{(x, y)\} + \text{mean}(w * C_V) \quad (6)$$

Here,

N_I denotes the normalized image.

w denotes the correlation weights.

Image Inpainting: It is the restoration of the statistically deteriorated sections of the image which should spatially match the rest of the image section. Impainting can be done in several ways including recent machine learning techniques or statistical estimation and interpolation [18]. One of the major challenges in this domain is to attain low computational complexity for the system and hence an Euclidean distance based interpolation method is adopted in this section. For this purpose, the pixel

correlation is computed for a patch of images wherein the inpainting is to be applied and is expressed as:

$$C_{patch} = \|P_T - P_C\|^2 \quad (7)$$

Here,

C_{patch} denotes the squared Euclidean norm for the patch.

P_T denotes the target patch.

P_C denotes the candidate patch.

In case of reconstruction, the inpainted patch pixels are weighed averages of the existing pixels satisfying the interpolation condition:

$$Z = \text{argmin}(P_T - P_C) \ll \text{mean}|P_S| \quad (8)$$

Here,

Z is the minimum interpolated difference co-efficient.

$\text{mean}|P_S|$ is the average pixel magnitude of the patch.

If the above condition is not satisfied, the inpainting is to be performed based on replacing the pixel values of the patch with the sum of average and consecutive standard deviations given by:

$$\mu + \frac{\sigma^2}{(\sigma+1)^2} \quad (9)$$

Here,

μ is the average pixel values.

σ is the standard deviation.

This type of interpolation allows to inpainted the image based on the estimation of both the mean pixel values as well as the extremities based on the standard deviations. This serves as a more robust technique compared to the conventional averaging approach. To identify the patch, the radial gradient of the fundus image is to be computed given by:

$$g_r = \frac{\partial}{\partial r} \phi_{r, x_0, y_0}^{r, x_f, y_f} \frac{I(x, y)}{2\pi r} ds \quad (10)$$

Here,

(x, y) denote image pixels

r denotes radius

g_r denotes radial gradient

Noise Removal: The next approach is the removal of the inherent noise effects in the image whose occurrence may the have following reasons [19].

- 1) Addition of electronic noise in the image due to the use of amplifiers in the sensing device which is also termed as white or Gaussian noise.
- 2) The abrupt change or spikes in the analog to digital converters sued in the circuitry of the fundus image causing salt and pepper noise patterns.

- 3) The multiplicative noise effect due to the inconsistent gain of the adaptive gain control (AGC) circuitry used for capturing or retrieving the fundus image^[20].
- 4) The lack of pixels while capturing the image resulting in frequency mean valued interpolations in the reconstructed image causing Poisson image^[21].

The removal of noise effects is fundamentally important as noisy images would result in erroneous feature extraction leading to inaccurate classification of the fundus images.

One of the most effective hyperspectral image restoration techniques is based on the sub-band decomposition of images into low pass and high pass signal values using the wavelet transform^[22]. The wavelet transform, unlike the conventional Fourier methods uses non-linear and abruptly changing kernel functions which show efficacy in analysing abruptly fluctuating signals such as images^[23]. The continuous and the discrete wavelet transforms are computed as^[24]:

$$CWT(x, s, \delta) = s^{\frac{1}{2}} \int_{-\infty}^{\infty} x(t) \phi^*\left(\frac{t-s}{\delta}\right) dt \quad (11)$$

Where,
 $s, \delta \in R$ represent the scaling (dilation) and shifting (translation) constants constrained to the condition $\delta \neq 0$.
 ϕ^* is the Wavelet Family or Mother Wavelet
 t is the time variable
 $x(t)$ is the time domain data.

For implementing the wavelet transform on the image dataset, the sampled version of the continuous wavelet transform yields the discrete wavelet transform given by:

$$DWT(x, m, n) = \delta_0^{\frac{-1}{2}} \sum_i x(i) \phi^*\left[\frac{n-is_0^m}{s_0^m}\right] \quad (12)$$

Where,
 $x(i)$ is the discrete $k \times 1$ vector.
 s_0^m is the discrete scaling constant.
 is_0^m is the discrete shifting constant.

The discrete wavelet transform yields two distinct low and high pass values based on the number of levels of decomposition and wavelet family given by the approximate co-efficient (CA) and detailed co-efficient (CD). The approximate co-efficient values are typically the low pass values containing the maximum information content of the image while the detailed co-efficient values account for the noisy spectral part^[25]. Retaining the low pass co-efficients and recursively discarding the high pass co-efficients allows to de-noise the image^[26]. The choice of the wavelet family impacts the estimation of the noise gradient vector given by:

$$G_N = k \frac{\nabla I}{\nabla I_F} \quad (13)$$

The value of the second order normalizing gradient as a function of spatial co-ordinates is given by:

$$q(x, y) = \sqrt{\frac{c_1(\nabla I/I_F)^2 + c_2(\nabla^2 I/I_F)^2}{(1+c_3(\nabla^2 I/I_F)^2)}} \quad (14)$$

Here,

I denotes the original image.

I_F denotes the fused image after normalization.

G_N denotes the normalizing gradient.

∇ represents the gradient.

∇^2 represents the Laplacian.

Feature Extraction: After the pre-processing and enhancement of the image is performed, the next process is the computation of statistical and texture based features from the image dataset. In recent literature it is found that a combination of both statistical and texture features are effective for classification problems^[27]. The features computed in the paper are^[28]:

$$Mean = \frac{1}{N} \sum_{i,j}^N f_{i,j} \quad (15)$$

$$s.d. = \sqrt{\frac{1}{N} \sum_{i,j}^N (f_{i,j} - mean)^2} \quad (16)$$

$$v = \frac{1}{N} \sum_{i,j}^N (f_{i,j} - mean)^2 \quad (17)$$

$$skewness = \sqrt[3]{\frac{1}{N} \sum_{i,j}^N (f_{i,j} - mean)^3} \quad (18)$$

$$Kurtosis = E\left[\left(\frac{x-mean}{s.d.}\right)^4\right] \quad (19)$$

$$rms = \frac{1}{n} \sqrt{\sum_{i=1}^n p_i^2} \quad (20)$$

$$Energy = \sum_{i,j}^N |p_{i,j}|^2 \quad (21)$$

$$Contrast = \sqrt{\frac{1}{mn} \sum_{i,j}^{m,n} [X(i, j) - mean\{X(i, j)\}]^2} \quad (22)$$

$$Corr_{2D} = \sum_{i,j}^{M,N} \frac{(i-m_x)(j-m_y)P_{x,y}}{sd_x sd_y} \quad (23)$$

$$E = -P[I_{x,y}] \log_2[[I_{x,y}]] \quad (24)$$

$$H = \sum_{i,j}^{M,N} \frac{P_{i,j}}{1-(i-j)^2} \quad (25)$$

$$smoothness = \frac{a}{1+a} \quad (26)$$

Here,

$f_{i,j}$ corresponds to the i^{th} colour component for pixel j
 $mean(m)$ denotes the average of the statistical features.

$s.d.$ denotes standard deviation

v denotes the variance

n denotes the number of pixels

p denotes the pixel value.

P denotes the probability of occurrence of pixel I w.r.t. pixel j .

$Corr_{2D}$ denotes 2-dimensional correlation

M & N denote the number pf pixels along x & y

m_x denotes mean along x

m_y denotes mean along y

sd_x denotes standard deviation along x

sd_y denotes standard deviation along y

Feature extraction serves as a serves the purpose of extracting empirical statistical information from raw data. The feature values defines in equations (15)-(26) serve as the parameters based on which any automated tool would classify a new fundus image sample as a positive or negative case of glaucoma^[29]. The veracity of the feature extraction process can be checked based on the correlation among the extracted features for a large dataset or a subset of the dataset. While individual image samples may exhibit divergences, yet the magnitude of such divergences in generally bound^[30]. Hence, a correlation among the extracted features would testify for the correctness of the feature extraction process and its applicability for pattern recognition by any automated classifier. The image enhancement and feature extraction process can be understood using the sequence of steps described in the proposed algorithm.

Classification

While designing a machine learning algorithm for automated glaucoma detection, the following constraints should be kept in mind:

1. Typically medical image data occupies large memory (compared to text or numerical data)
2. For medical applications, the memory and processing power of the equipments would be limited. Thus the algorithm should NOT possess high computational complexity.
3. The SCG algorithm is fast and relative less computationally complex and hence is well suited for large medical image data analysis.

The scaled conjugate gradient tries to find the steepest descent vector prior to weight update in each iteration and is mathematically given by:

$$A_0 = -g_0 \quad (27)$$

Here,

A is the initial search vector for steepest gradient search

g is the actual gradient

$$w_{k+1} = w_k + \mu_k g_k \quad (28)$$

Here,

w_{k+1} is the weight of the next iteration and w_k is the weight of the present iteration

μ_k is the combination co-efficient

For any iteration k , the search vector is given by:

$$A_k = -g_k + \beta_k A_{k-1} \quad \beta_k = \frac{(|g_{k+1}|^2 - g_{k+1}^T g_k)}{g_k^T g_k} \quad (29)$$

Here,

The customary g represents $\frac{\partial e}{\partial w}$

Proposed Algorithm:

Start.

Step. 1: Load image of interest.

Step. 2: Employ RGB-Grayscale conversion.

Step.3: Identify patch to be inpainted based on the contour 'C' enclosed by the gradient:

$$g_r = \frac{\partial}{\partial r} \oint_{r, x_0, y_0}^{r, x_f, y_f} \frac{I(x, y)}{2\pi r} ds$$

Step. 4: Compute: $argmin(P_T - P_C)$

Step.5:

if ($argmin(P_T - P_C) \ll mean|P_S|$)

Replace patch with $mean|P_S|$

else

Replace patch with:

$$\frac{1}{n} \left(\sum_{i=1}^n \mu + \frac{\sigma^2}{(\sigma + 1)^2} \right)$$

Step.6: For illumination correction, compute the convolution of the Gaussian kernel and the original image bounded by the contour 'C'.

}

Step.7: Compute:

$$|kI - I_C|$$

Step.8: Generate fused images as:

$$I_F = wC_{V-norm}I + I_C$$

Step.9: Decide decomposition levels ' n ' and family of wavelet function.

Step.10: Compute the normalizing gradient as:

$$q(x, y) = \sqrt{\frac{c_1(\nabla I/I_F)^2 + c_2(\nabla^2 I/I_F)^2}{(1 + c_3(\nabla^2 I/I_F)^2)}}$$

Step.11: *for* $i = 1:n$
retain C_A *and discard* C_D

Step.12: Compute the Normal and Cumulative Histograms of the original and de-noised images, along with the histogram metrics.

Step.13: Compute Feature Distribution over the entire range of image index.

Step.14: Train the SCG based deep neural network, and truncate training on convergence.

Step.14: Test Network

Step.16: Computer Classification Accuracy
Stop.

RESULTS AND DISCUSSIONS

For the purpose of this study, 1000 images comprising of both positive and negative cases of glaucoma have been obtained from the Kaggle dataset^[12]. The images acquired are .jpg images which three colour channels viz. R, G and B. The image enhancement and feature extraction has been performed on Matlab 2020a, with a RAM of 8GB and an i5-9300H CPU. All the images are first converted to common dimensions of (256 x 256) The results have been presented subsequently.

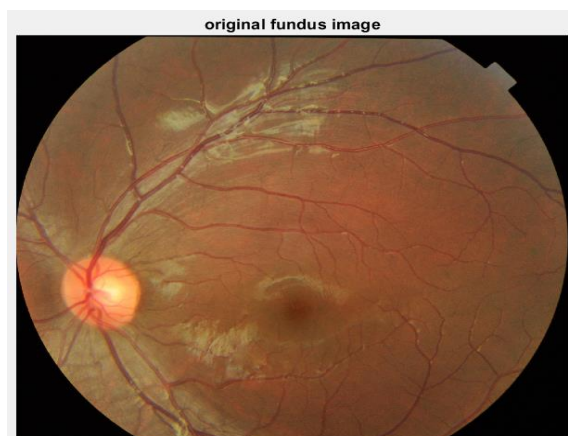


Fig.2. Original fundus image

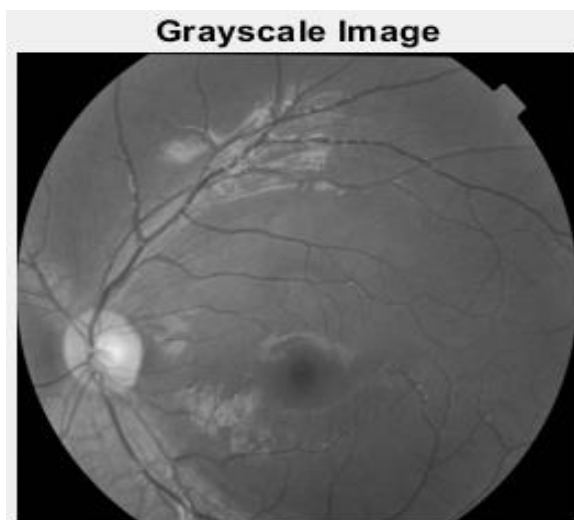


Fig.3 Grayscale Image

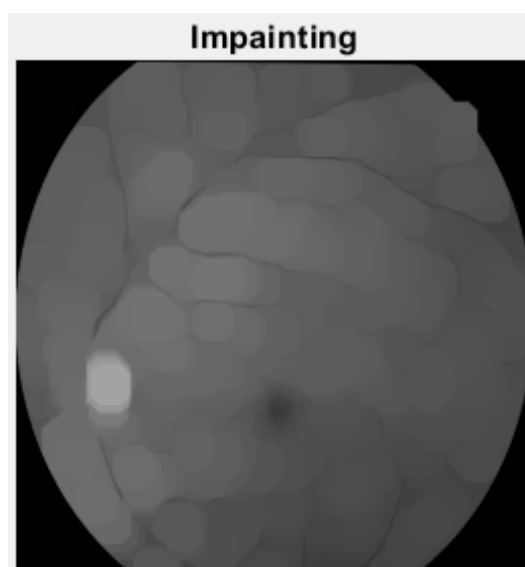


Fig.4 Applying image inpainting

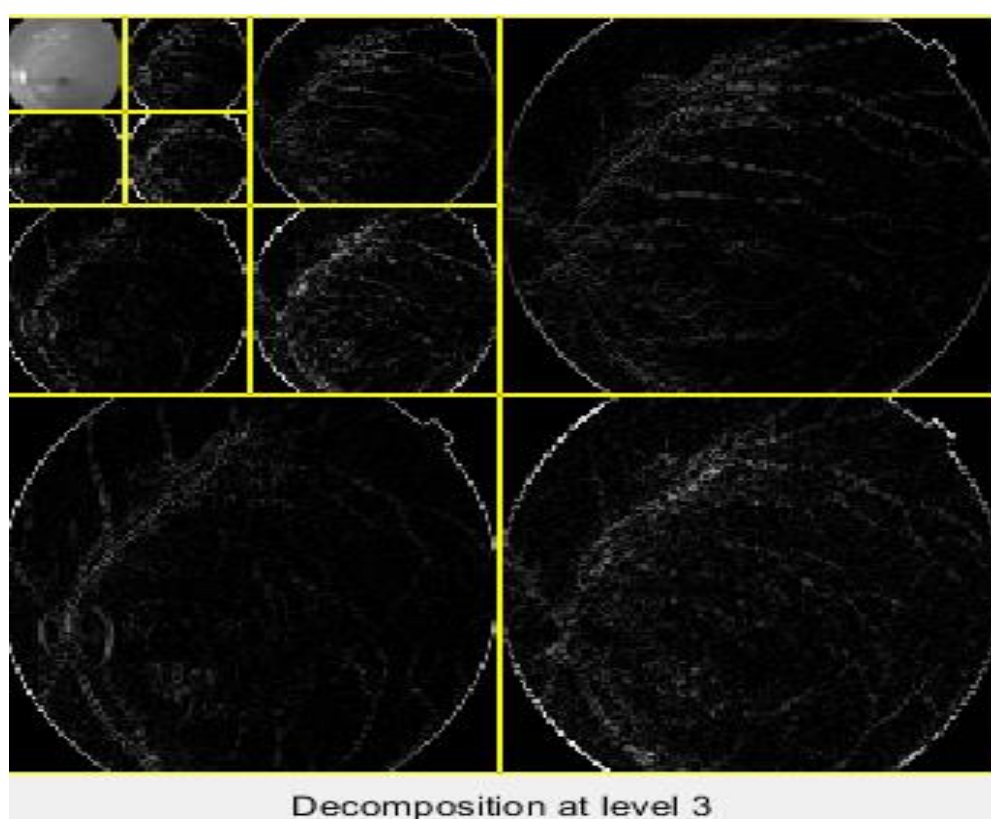


Fig.5 Haarlet decomposition at level 3.

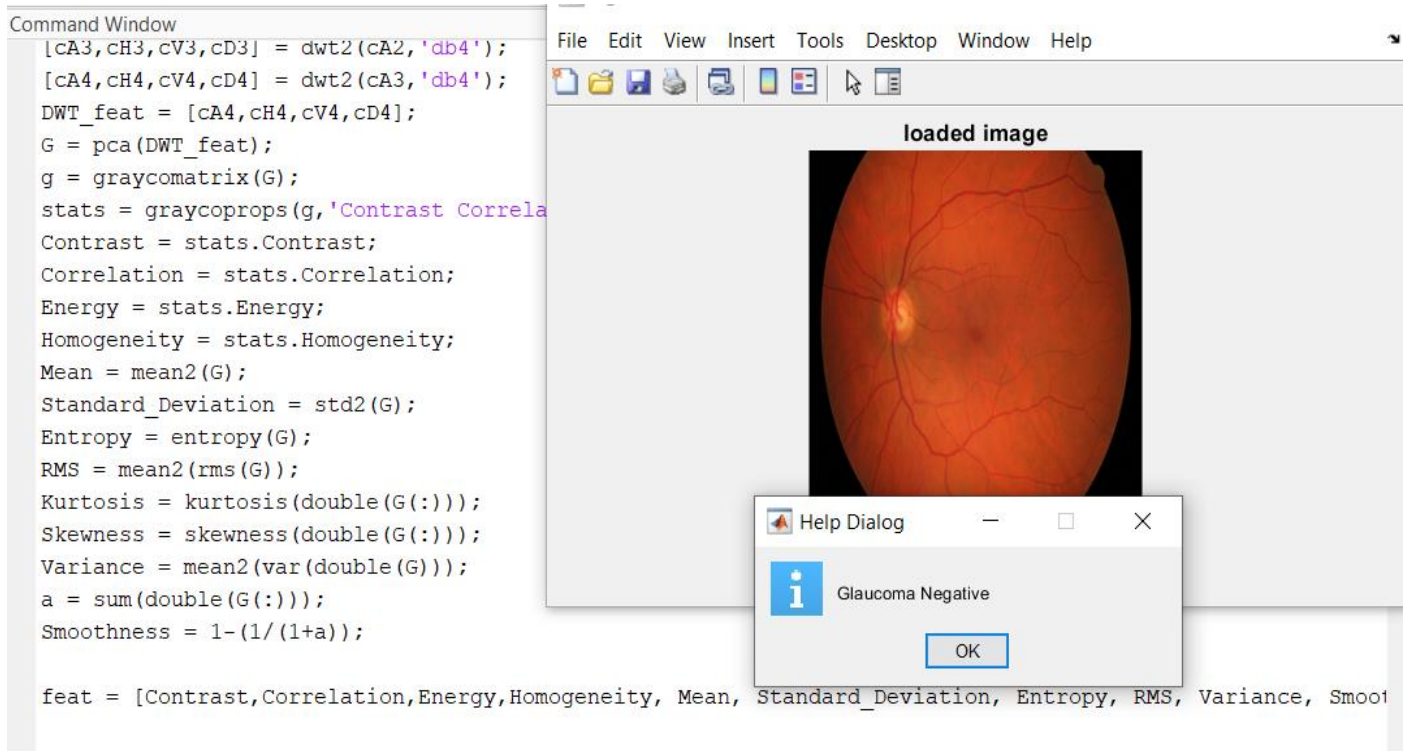


Fig. 6. Classification GUI

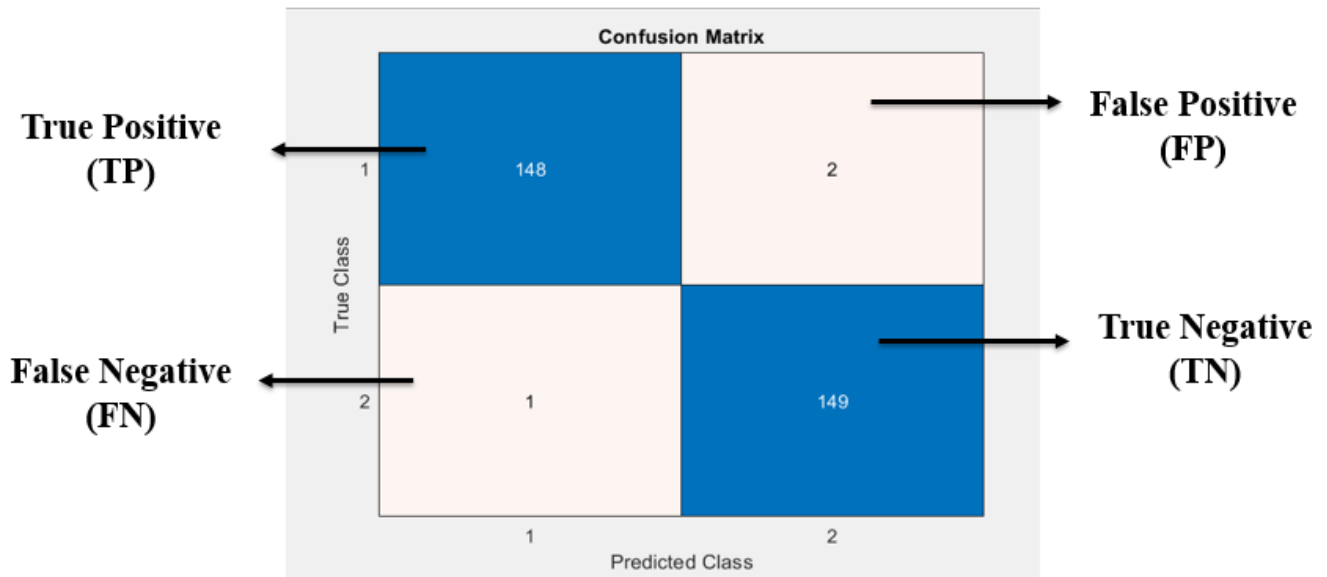


Fig. 7. Confusion Matrix

Figure 7 depicts the confusion matrix. The classification accuracy is computed as:

$$Ac = \frac{TP + TN}{TP + TN + FP + FN} = \frac{\text{Correct Decisions}}{\text{Total Decisions}}$$

$$Accuracy = \frac{148 + 149}{148 + 149 + 2 + 1} = 98.5\%$$

A comparison with Nayak et al. [31] (accuracy of 97.2%) and Wu et al. [32] (accuracy of 85%) clearly indicates that the proposed work outperforms the existing baseline techniques in terms of classification accuracy.

CONCLUSION

It can be concluded from the previous discussions that it is necessary to design accurate automated tools for detection of glaucoma to inhibit the progression of the disease resulting in visual impairments and blindness. The design of automated systems, however face the challenge of the raw data being prone to noise and disturbance effects while capturing, retrieval and sharing. Moreover, the statistical features of the raw data for both positive and negative cases of glaucoma show similarity making automated accurate classification challenging. This paper presents an algorithm which first pre-processes the raw images to correct illumination inconsistencies followed by a recursive discrete wavelet transform based approach for noise removal. Subsequently, a feature extraction mechanism is proposed which is capable of computing both texture and statistical features from the images. The results show that the proposed approach attains both noise removal and coherence in feature extraction from the fundus images and serves a critical tool for accurate and automated glaucoma detection. The proposed approach presents an approach comprising of statistical feature selection and probabilistic neural network. The

accuracy achieved by the proposed technique is 98.5% which is significantly higher than the existing approach.

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