

# K-MAP

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## ABSTRACT:

This research paper mainly focuses on an important topic of digital electronics that is the k map , how to solve the kmap, Steps to solve kmap using expression, it's SOP format, How does kmap works, What are kmap rules.

## WHAT IS K-MAP?

A K-Map (or Karnaugh Map) is a graphical representation of a Boolean function used to simplify Boolean algebra expressions. It is a two-dimensional grid of cells, each representing a possible combination of inputs to the Boolean function. The cells are colored or labeled according to the output of the function for that particular combination of inputs. By visually grouping together cells with similar outputs, one can simplify the Boolean expression and reduce the number of logic gates required to implement the function.

In many digital circuits and practical problems we need to find expression with minimum variables. We can minimize Boolean expressions of 3, 4 variables very easily using K-map without using any Boolean algebra theorems. K-map can take two forms Sum of Product (SOP) and Product of Sum (POS) according to the need of problem. K-map is table like representation but it gives more information than TRUTH TABLE. We fill grid of K-map with 0's and 1's then solve it by making groups.

The K-Map provides a visual representation of the Boolean function that can be used to simplify the expression and reduce the number of variables. By grouping cells with similar outputs, the function can be expressed in a more simplified form, either as a Sum of Products (SOP) or a Product of Sums (POS) expression. The K-Map can provide more information than a truth table and can be a useful tool for minimizing Boolean expressions, especially for larger expressions with 3 or 4 variables.

## STEPS TO SOLVE THE KMAP:

Steps to solve expression using K-map- Select K-map according to the number of variables. Identify minterms or maxterms as given in problem. For SOP put 1's in blocks of K-map respective to the minterms (0's elsewhere). For POS put 0's in blocks of Kmap respective to the maxterms(1's elsewhere). Make rectangular groups containing total terms in power of two like 2,4,8 ..(except 1) and try to cover as many

elements as you can in one group. From the groups made in step 5 find the product terms and sum them up for SOP form

1. Choose the appropriate K-Map based on the number of variables..
2. Determine whether you need to use minterms (for SOP) or maxterms (for POS) based on the problem.
3. the K-Map with 1's for SOP (at the locations of the minterms) or 0's for POS (at the locations of the maxterms).
4. Group cells together to form rectangles that contain a number of terms equal to a power of two.
5. From the groups, determine the product terms and sum them up to obtain the simplified Boolean expression in SOP or POS form.

SOP FORM 1. 3 variables K-map:  $Z = \sum P, Q, R (1, 3, 6, 7)$

The 3-variable K-Map for  $Z = \sum (1, 3, 6, 7)$  in SOP form would look like this:

<b>P\Q R</b>	<b>0 1</b>
0 0	0 1
0 1	1 1
1 0	0 1
1 1	1 0

of inputs. By grouping cells with similar outputs together, one can simplify the Boolean expression and reduce the number of variables.

The minterms (1, 3, 6, 7) are represented by the cells that are marked with a 1 in the KMap. To find the simplified Boolean expression, we can group cells together to form rectangles that contain a number of terms equal to a power of two. In this case, the groups can be (1,3) and (6,7), and the simplified Boolean expression can be expressed as:

$$Z = P'Q + PR$$

This is the SOP form of the expression for the function Z.

In the SOP form, the cells are filled in with 1's for the minterms of the function. By grouping cells together to form rectangles that contain a number of terms equal to a power of two, one can obtain a simplified Boolean expression in SOP form by finding the product terms and summing them up.

In the POS form, the cells are filled in with 0's for the maxterms of the function. By

Grouping cells together to form rectangles

The K-Map method works by providing a visual representation of a Boolean function, where each cell in the K-Map corresponds to a possible combination of inputs to the function. The cells are then filled in with the output of the function for that combination

How does k map method works? That contain a number of terms equal to a

Power of two, one can obtain a simplified Boolean expression in POS form by finding the sum terms and multiplying them.

For larger expressions with 3 or more variables.

The K-Map method provides a more efficient and visual way of simplifying Boolean expressions compared to using Boolean algebra theorems alone, especially

There are several rules to follow when using a K-Map to simplify Boolean expressions:

Rectangles that contain a number of terms equal to a power of two, one can simplify the Boolean expression in either SOP or POS form. Following the rules of K-Map such as adjacent cells, rectangular grouping, number of terms, consistent labeling, summing or multiplying terms, and simplicity can lead to an efficient and effective solution. The KMap method is particularly useful for simplifying Boolean expressions with 3 or more variables.

1.        Adjacent cells: Adjacent cells in a KMap must correspond to combinations of inputs that differ in only one variable.
2.        Rectangular grouping: The cells in the K-Map should be grouped together to form rectangles that contain a number of terms equal to a power of two.
3.        Number of terms: The number of terms in a group should be minimized, with larger groups preferred over smaller groups.
4.        Consistent labeling: The cells in a group should be labeled consistently, either all 1's or all 0's.
5.        Summing terms: For the SOP form, the product terms for each group should be determined and summed up to obtain the simplified Boolean expression.
6.        Multiplying terms: For the POS form, the sum terms for each group should be determined and multiplied together to obtain the simplified Boolean expression.
7.        Simplicity: The goal of the K-Map method is to simplify the Boolean expression, so the final expression should be as simple as possible.

Conclusion for the above Article:

In conclusion, K-Map is a useful method for simplifying Boolean expressions in digital circuits and practical problems. It provides a visual representation of a Boolean function by filling in a grid with 0's and 1's according to the minterms or maxterms of the function. By grouping cells together to form