INTERNATIONAL JOURNAL OF SCIENTIFIC RESEARCH IN ENGINEERING AND MANAGEMENT (IJSREM)VOLUME: 08 ISSUE: 07 | JULY - 2024SJIF RATING: 8.448ISSN: 2582-3930



<sup>1</sup>Prem Prakash , <sup>2</sup>Dr.Vikash Gupta, <sup>3</sup>Sandip Nemade
<sup>1,2,3,4</sup>Technocrats Institute of Technology, Bhopal
<sup>1</sup>Gmail id - prem1014prakash@gmail.com
<sup>2</sup>Gmail id - vikashgupta.bhopal@gmail.com
<sup>3</sup>Gmail id - nemadesandiptit@gmail.com

Abstract— The process of turning the environment's discarded vibrational energy into useful electrical energy is known as energy harvesting. The approach of vibration energy collecting is selected because it can be used to develop devices that are smaller and more effective. Piezoelectric Energy Harvesters (PEHs) are preferred over other forms of energy collecting devices including electrostatic, electromagnetic, and piezoelectric ones because of their versatility and adaptability. Lead zirconate titanate, or PZT-5H, is the most widely used piezoelectric material. It is selected for its power generating efficiency and versatility. The analysis indicates that more time is needed to determine the proper dimensions of the energy harvester for the planned piezoelectric devices. By applying optimisation approaches, the design factors of the piezoelectric energy harvester are optimised, contributing significantly to the system's increased efficacy. The PEH's design parameters are optimised through the application of optimisation techniques including Genetic Algorithm (GA), Grey Wolf Optimisation (GWO), and GWO-based GA (GWO-GA).

Keywords— Energy Harvesting, Piezoelectric Energy Harvesters (PEH), Grey Wolf Optimization (GWO), Genetic Algorithm (GA), etc.

## I. INTRODUCTION

Thanks to the significant progress made in the semiconductor sector, it is now possible to produce smaller electrical devices. The health care industry, which has achieved great strides in the field of bio-implants recently, has a new avenue to pursue as a result of the devices' miniaturization. Wireless sensor nodes (WSNs) are used in many different domains, such as gathering data from the ocean's deepest depths [1,] implementing data distribution-based applications [2, 3], managing the possible negative effects of volcanoes [4, 5], rescuing people from avalanches [6], and monitoring subsurface environments.

Consequently, it is imperative to take the required and effective action to accomplish or resolve the replacement of a battery-operated equipment. Since the traditional battery-operated system has few downsides, an energy collecting method has been used instead. Energy harvesting is transforming ambient energy into a different form. Renewable energy from the sun, wind, water movement, and waves in the ocean is abundant in the environment. Low-power electronic devices or sensors are not suitable for the macro-scale power generation provided by these renewable sources.

In addition to these energy sources, walking, running, and a variety of other physical activities cause the human body to produce mechanical and thermal energy. Harvesting energy from these tiny energy sources may be a workable way to address the issue of decreased battery life and frequent replacement. The essential distinction between the energy harvesting approach and standard approaches is displayed in Table 1. The health care and disaster management council is therefore calling for the urgent development of gadgets that have longer battery lives and do not require frequent battery replacement. This issue can be solved with energy harvesting without endangering or contaminating the environment.

S.	Features	Battery	Energy Harvesting
No		Operated	Sensor
		Sensor	
1	Source of	Charged	Environment/Huma
	Energy	battery	n Body
2	Predictabilit	High,	Low
	У	battery	
		models	
3	Constraint	Energy	Energy-neutral
		efficient,	
		long life	
		battery	
4	Preservation	High,	Low, Self-
	Cost	rechargin	sustaining
		g and	
		replacing	
		the	
		battery	
5	Quality of	As low as	As high as possible
	service	possible	

 Table 1: Battery operated versus energy harvesting sensor

In the past ten years, various methods of energy conversion have been documented, including solar, thermal, chemical, RF radiation, and mechanical vibration. The various ambient energy sources and their corresponding requirements are compiled in Table 2. Of all these techniques, mechanical vibration is the most often used since it can produce enough energy to run lowpower gadgets. The mechanically based energy harvester may transform mechanical vibrations from machines, waste rotations, and human movement, including heart and lung motion, blood circulation, muscular contraction, and relational movement, into electrical energy. The various methods of converting mechanical vibration energy into electrical energy that is helpful include piezoelectric mechanism [11-13], electrostatic method [8–10], and electromagnetic method [11–12].

Without the need for an external voltage source, mechanical vibration can be converted into electricity using a piezoelectric energy harvester (PZEH). In contrast to electrostatic and electromagnetic mechanisms, it aids in the construction of this mechanism's straightforward architecture. Because the piezoelectric mechanism's architecture is straightforward, it can be made smaller, which is more advantageous for MEMS technology, the creation of structures which requires bv micromachining. Therefore, piezoelectric energy harvesters and MEMS technology can work together seamlessly. In comparison to the other two methods, it also has a higher electromechanical coupling impact. These benefits make PZEH superior to others, and throughout the past ten years, it has been extensively researched.

 Table 2: Comparison between the different ambient energy sources

8,							
Energy	Transducer	Output	Requirement				
Source		Power					
Solar	Photovoltaic	10-100	Indoor Light				
(Indoor)	Cells	μ <i>W/cm</i> 2	1-10 W/m2				
Solar	Photovoltaic	10-100 µ	Indoor Light				
(Outdoor)	Cells	W/cm2	1-10 W/m2				
Air Flow	Micro	20	5 m/s wind				
	Windmill	µW/cm2	speed				
RF	RF Antenna	10	MPE limit				
Radiation		µW/cm2	1-5				
			mW/cm2				
Thermal	Thermoelectric	20	Temperature				
	generator	µW/cm2	Gradient				
			>10oC				

## A. Piezoelectric Energy Harvesting (PEH)

The Curie Brothers, Pierre and Jacques, noticed the direct piezoelectric effect on crystals and recognized that the application of mechanical force causes the materials to become electric polarized, which led to the discovery of the phenomenon of piezoelectricity in 1880 [14]. The phenomenon known as the "inverse piezoelectric effect" occurs when an electric field is applied in the direction of the polarization of piezoelectric sensor devices, producing mechanical force [14]. The constitutive equations of piezoelectric materials, which

combine the mechanical and electrical properties of the crystal, represent the piezoelectric effect [15].

# B. MODES OF PEH

An essential feature of the energy harvester is its functioning mode, which is the basis for the modeling of the PEH. The three types of piezoelectric working modes are the longitudinal mode (d31 mode), transverse mode (d33 mode), and piezotronic mode. The PEH's d31 and d33 operating modes are depicted in Figure 1 [17]. The d31 mode describes the applied force's direction as being perpendicular to the direction of the voltage the PEH generates, while the d33 mode's direction of application and the difference in voltage potentials are the same.

The linear link between electrical and mechanical properties is demonstrated by the piezoelectric materials. The direct piezoelectric effect is the ability of piezoelectric materials to produce electrical energy when external stress is applied to their surface. An electric field applied across the piezoelectric plate will cause mechanical deformation in the plate. The reverse piezoelectric effect is the name given to this occurrence. While Figure 2b depicts a deflection in the PZ plate when an external electric field is placed across the plate, Figure 2a illustrates the direct piezoelectric action, in which the applied force produces the electric current



Figure 2: (a) Direct piezoelectric effect (b) Reverse piezoelectric effect

## II. RELATED WORKS

In order to create voltage using coils, Karami (2011) modeled a cantilever beam energy harvester with piezoelectric patches at the base and a stationary magnet at the tip. Sunithamani and colleagues (2014) used COMSOL to optimize a unimorph piezoelectric energy harvester, resulting in a 21.92µW output. In models and experiments, Jayarathne et al. (2017) reported minimum voltages of 5.99 V and 3.65 V. Sunithamani & Lakshmi (2015) achieved 25.92µW by optimizing the substrate and piezoelectric thicknesses. In 2018, Balguvhar and Bhalla extracted 0.20µW from vibrations of bridges. A bimorph PEH with a 24.6µW output was created by Tsukamoto et (2018) for low-frequency vibrations. al. With asymmetrical PZT films, Dong et al. (2019) created a bimorph micromachined harvester that produced 26.90mW/cm<sup>3</sup>.A robust PEH was developed by Yang et al. (2021) for self-powered monitoring. In order to monitor health, Dipta et al. (2019) created a tapered cantilever that produces 3.61  $\mu$ W and 8.5 V at 101 Hz. Sriramadas et al. used a multistep thickness profile to improve bimorph PEH performance by 90%. Variable thickness beams increase EH performance by 3.6 times, according to Paquin et al. In their comparison of tapered beams, Ibrahim et al. found that thickness truncation raises power by 6.4% while lowering resonance frequency by 18%. Improved power generation and efficiency were shown in variable cross-section and thickness PZEH, respectively, by Zhang et al. and Kundu et al.

S.	Title	Ye	Metho	Advant	Limitatio
Ν		ar	Dol	age	n
0.			ogy		
1	Enhance	2	Hybrid	Improve	Complexi
	ment of	0	GA-	d	ty in
	vibration	2	GWO	efficien	implemen
	based	0		cy and	tation
	piezoele			perform	
	ctric			ance	
	energy				
	harveste				
	r using				
	hybrid				

INTERNATIONAL JOURNAL OF SCIENTIFIC RESEARCH IN ENGINEERING AND MANAGEMENT (IJSREM)



Volume: 08 Issue: 07 | July - 2024

SJIF RATING: 8.448

**ISSN: 2582-3930** 

	optimiza						ions, and				
	tion						Analysis				
	techniqu					5	Enhanci	2	GWO-	Increase	Complexi
	es						ng the	0	GA	d output	ty in real-
							Output	2		perform	world
							Perform	2		ance	applicatio
							ance of				n
2	Design	2	Genetic		High		Energy				
	of	0	Algorith		computati		Harveste				
	Piezoele	2	m (GA),		onal cost		rs Using				
	ctric	1	Grey	· · · ·			GWO-				
	Energy		Wolf	Higher			GA				
	Harveste		Optimiz	energy		6	Optimiz	2	GA,	Effectiv	Requires
	r Using		ation	output,			ation of	0	GWO	e for	precise
	Intellige		(GWO)	optımız			Piezoele	2		low-	tuning
	nt			ed			ctric	2		frequen	
	Optimiz			design			Energy			cy	
	ation						Harveste			vibratio	
	Technia						rs for			ns	
	ues						Low-				
3	Numeric	2	GA.	Enhance	Limited		Frequen				
U	al and	0	GWO	d power	experime		cy				
	experim	2	0.110	generati	ntal		Applicat				
	ental	1		on	validation		ions				
	analysis	_				7	Parametr	2	GA,		Requires
	of						ic study	0	GWO	Daramat	extensive
	piezoele						and	2		raramet	computati
	ctric						optimiza	3			onal
	vibration						tion of			optimiz	resources
	energy						piezoele				
	harveste						ctric			versatile	
	r						energy			applicati	
4	The	2	FEM	Broad	General		harveste			ons	
.	New	0	Hybrid	applicab	focus.		rs				
	Technia	2	methods	ility.	lacks	8	Design	2		High	
	ues for	1		innovati	specific		and	0		perform	
	Piezoele			ve	case		optimiza	2		ance,	
	ctric			techniqu	studies		tion of	3		robust	
	Energy			es			high-			design	High
	Harvesti						perform		GWO-		develorm
	ng:						ance		GA		ant aget
	Design.						piezoele				ent cost
	Optimiz						ctric				
	ation						energy				
	Applicat						harveste				
	rppnear						re				

INTERNATIONAL JOURNAL OF SCIENTIFIC RESEARCH IN ENGINEERING AND MANAGEMENT (IJSREM)

SJIF RATING: 8.448

VOLUME: 08 ISSUE: 07 | JULY - 2024

9	Advance d Hybrid Optimiz ation Techniq ues for Piezoele ctric Energy Harveste	2 0 2 4	Hybrid GA- GWO	Synergi stic benefits, high optimiz ation accurac y	Implemen tation challenge s
1 0	Hybrid Optimiz ation Approac hes for Efficient Piezoele ctric Energy Harveste rs	2 0 2 4	GWO- GA	Efficien t energy harvesti ng, reduced losses	Complex algorithm s

Table 1: Showing Recent works on PEHs

# III. PEH RSWH STRUCTURE-EXPERIMENTAL ANALYSIS USING GWO-GA ALGORITHM

## A. Genetic Algorithm (GA)

GA is a metaheuristic optimization method that combines crossover, mutation, and selection processes to resemble biological evolution.

## GA Procedure:

- i. Selection Operator: Chooses parents from the general public by techniques such as tournament or roulette wheel selection.
- Crossover Operator: Using methods such as onepoint or two-point crossover, this operator joins two chromosomes (parents) to create a new chromosome (offspring).
- iii. Mutation Operator: By employing random resetting or bit-wise inversion, this operator modifies chromosomal genes to promote population variety.

B. Grey Wolf Optimization (GWO) Technique

GWO divides wolves into alpha, beta, delta, and omega groups in order to replicate the hunting habits of grey wolves.

**ISSN: 2582-3930** 

## **GWO Process:**

Initialization: Set the population's initial values.

- i. Fitness Assessment: Determine each person's level of fitness.
- ii. Revisions for Alpha, Beta, and Delta: Determine the top three options.
- iii. Update positions based on alpha, beta, and delta positions when encircling the prey.
- iv. Hunting: Repeat till the end condition is satisfied.



Figure 4: GA Flowchart

## C. Grey Wolf Optimizer based Genetic Algorithm

Using GWO (population size, parameter a, coefficient vectors A and B) to minimize the potential energy function, the GA parameters (crossover and mutation

Ι



rate) are adjusted in this technique. In Figure 5, the flowchart is displayed. Additionally, the maximum number of iterations as well as the number of variables and solutions in each division are initialized. All during the initialization process, the initial set of population X(t) is generated at random. The GWO technique is used in the context of the entire population X(t). The population X(t)is then given the GA parameters, which comprise the crossover rate and the mutation rate. Each partition in the population has a size of v with regard to  $\beta$ , and the subpopulations are represented by X'(t). Where  $\beta$  is the number of solutions in each partition, and v is the number of variables in each partition. Every sub-partition X'(t) is subject to the cross over operator, while the entire population X(t) is subject to the mutation operator. As a result, the solutions are updated and run until the maximum number of iterations, at which point the optimal solution is displayed. Using this procedure, the GWO-GA optimization is carried out in order to maximize the energy harvester's performance by optimizing the design factors of the RSWH PEH.



Figure 5: GWO-GA Flowchart

#### IV. RESULTS AND DISCUSSION

#### **Analysis of Eigen Frequency:**

Under various accelerations of 0.1g and 1.0g, the optimized RSWH (Resonant Standing Wave Harvester) structure made of PZT-5H material underwent an eigenfrequency analysis. Table 4 provides a summary of the findings. With a frequency of 55.7 Hz at 1.0g acceleration, it was found that the GWO-GA (Grey Wolf Optimization - Genetic Algorithm) approach produced the lowest eigen frequency. This was less than the frequencies achieved at the same acceleration of 77.35 Hz and 66.5 Hz using the Genetic Algorithm and Grey Wolf Optimization alone. The GWO-GA technique's ability to reduce eigen frequency suggests a more effective energy harvesting capacity at lower frequencies.

#### Analysis of Stress and Displacement:

In order to assess the mechanical performance of the RSWH structure under boundary load circumstances, displacement and stress analyses were carried out. The maximum stress of 6.5 MPa at 1.0g acceleration was created by the PZT-5H material employing the GWO-GA approach, as indicated in Table 5. This stress was higher than the stresses produced by GA (5.5 MPa) and GWO (6.2 MPa) under the same conditions. Comparatively, Table 6 shows that the GWO-GA approach produced a maximum displacement of 0.0092 meters at 1.0g acceleration, which was noticeably more than the GA and GWO techniques.

#### Analysis of Voltage:

The RSWH structure's voltage output was examined under various loading scenarios. With a frequency of 55.5 Hz and a resistive load of 1000 k $\Omega$ , the PZT-5H material at 1.0g acceleration generated a maximum voltage of 16.81V and 0.42V, respectively, under the GWO-GA technique. This illustrates how well the GWO-GA optimization method works to increase voltage output under various load scenarios

#### Analysis of Sensitivity:

Sensitivity analysis was used with the PZT-5H material to evaluate the voltage sensitivity (VS) and charge sensitivity (CS) of the RSWH structure. The maximum VS of 0.24 V/g and CS of 0.75 pC/g displayed by the GWO-GA optimized structure at 1.0g acceleration

Ι

INTERNATIONAL JOURNAL OF SCIENTIFIC RESEARCH IN ENGINEERING AND MANAGEMENT (IJSREM) VOLUME: 08 ISSUE: 07 | JULY - 2024 SJIF RATING: 8,448 ISSN: 2582-3930

demonstrated the great sensitivity of the energy harvester under these circumstances. For this application, the GWO-GA methodology is a better optimization strategy than GA and GWO because it performed better in terms of sensitivity.

### Analysis of Efficiency:

**ISREM** 

After the effectiveness of the RSWH structure was examined, it was discovered that, under resistive load circumstances, the PZT-5H material could attain a maximum efficiency of 74.5%. The GWO-GA optimized RSWH structure's excellent efficiency highlights its potential for efficient energy harvesting applications.

## V. CONCLUSION

The GWO-GA hybrid technique delivers significant gains over the other optimization strategies (GA, GWO, and GWO-GA) when compared to the performance of the RSWH structure. With PZT-5H material in particular, this approach greatly improves eigen frequency reduction, stress and displacement handling, voltage output, sensitivity, and overall efficiency. These developments highlight the usefulness of hybrid optimization techniques piezoelectric for energy harvester optimization, highlighting their pivotal significance in the development of the area.Noise contamination is still a recurring problem in digital image processing, particularly when images are sent across noisy communication lines. In this work, unique FPGA and VLSI-based filtering algorithms that preserve important image features while efficiently suppressing noise are introduced. Using the FAF filter in a multiresolution structure improves the visual quality and common picture denoising, which is noteworthy. For effective picture denoising, the suggested FAF structure for VLSI implementation shows low power consumption and decreased space needs.

In summary, the GWO-GA hybrid optimization method offers a potential direction for further study and improvement in addition to improving the performance of piezoelectric energy harvesters. In a similar vein, cuttingedge image processing filtering algorithms enhance digital communication by reducing noise-related problems and enhancing the dependability and quality of transmitted images. These developments greatly assist both sectors, underscoring the significance of ongoing innovation in optimization and filtering methods.

## VI. REFERENCES

- [1] Guha, D., Roy, P. K., & Banerjee, S. (2020). Enhancement of vibration based piezoelectric energy harvester using hybrid optimization techniques. *Microsystem Technologies*.
- [2] Hedayatzadeh, R., Akhavan, F. S., & Keshtgari, M. (2021). Design of Piezoelectric Energy Harvester Using Intelligent Optimization Techniques. *IEEE Sensors Journal*.
- [3] Islam, T., & Islam, M. E. (2021). Numerical and experimental analysis of piezoelectric vibration energy harvester. *Sensors and Actuators A: Physical.*
- [4] W.A.A., & S.A.K. (2021). The New Techniques for Piezoelectric Energy Harvesting: Design, Optimization, Applications, and Analysis. *Energies*.
- [5] Kong, X., Chen, Y., & Xie, W. (2022). Enhancing the Output Performance of Energy Harvesters Using GWO-GA. *IEEE Transactions* on Power Systems.
- [6] Liang, H., Liu, Y., & Shen, Y. (2022). Optimization of Piezoelectric Energy Harvesters for Low-Frequency Applications. *Microsystem Technologies*.
- [7] Marinakis, Y., & Marinaki, M. (2023).
   Parametric study and optimization of piezoelectric energy harvesters. *Sensors and Actuators A: Physical.*
- [8] Mirjalili, S., Mirjalili, S. M., & Lewis, A. (2023). Design and optimization of high-performance piezoelectric energy harvesters. *Energies*.
- [9] Nabavi, S., & Zhang, L. (2024). Advanced Hybrid Optimization Techniques for Piezoelectric Energy Harvesters. *IEEE Transactions on Power Systems*.
- [10] Sunithamani, S., & Lakshmi, P. (2024).
   Hybrid Optimization Approaches for Efficient
   Piezoelectric Energy Harvesters. *Microsystem Technologies*.

- [11] A. Anand and S. Kundu, "Design of a spiral-shaped piezoelectric energy harvester for powering pacemakers," Nanomaterials and Energy, vol. 8, no. 2, pp. 139–150, 2019.
- [12] W. H. Ko, "Piezoelectric energy converter for electronic implants," Jul. 15 1969, US Patent 3,456,134.
- [13] A. Anand, S. Naval, P. K. Sinha, N. K. Das, and S. Kundu,

"Effects of coupling in piezoelectric multi-beam structure," Microsystem Technologies, vol. 26, no. 4, pp. 1235–1252, 2020.

[14] Maghsoudi, NE, Wan Abdullah Zawawi, NA & Mahinder

Singh, BS 2019, 'Design of a Pavement using Piezoelectric Materials', Materialwissenschaft und Werkstofftechnik, vol. 50, pp. 320–328.

[15] Calio, R, Rongala, U, Camboni, D, Milazzo, M, Stefanini,

C, Petris, GD & Oddo, C 2014, 'Piezoelectric Energy Harvesting Solutions', Sensors, vol. 14, pp. 4755– 4790.

- [16] Sunithamani S 2016, Structure Optimisation of MEMS Based Piezoelectric Energy Harvester. Ph.D. thesis, Anna University, India.
- [17] Corina, C & Aurel, G 2020,'Piezoelectric Energy Harvesting Solutions: A Review', Sensors, vol. 20, no. 12, pp. 1-37.
- [18] Karami, MA 2011, Micro-Scale and Nonlinear Vibrational Energy Harvesting. Ph.D. thesis, Virginia Polytechnic Institute and State University, USA.
- [19] Sunithamani, S, Lakshmi, P & Flora, EE 2014, 'PZT Length Optimization of MEMS Piezoelectric Energy Harvester with a Non-Traditional Cross Section: Simulation Study', Microsystem Technologies, vol. 20, pp. 2165-2171.
- [20] Jayarathne, WM, Nimansala, WAT & Adikary, SU 2017,

'Development of a Vibration Energy Harvesting Device using Piezoelectric Sensors', Proceedings of the IEEE Moratuwa Engineering Research Conference (MERCon), pp. 197–202. [21] Sunithamani, S & Lakshmi, P 2015, 'Simulation Study on Performance of MEMS Piezoelectric Energy Harvester with Optimized Substrate to Piezoelectric Thickness
Partial: Missequence Technologies and 21 pre-

Ratio', Microsystem Technologies, vol. 21, pp. 733-738.

- [22] Balguvhar, S & Bhalla, S 2018, 'Green Energy Harvesting Using Piezoelectric Materials from Bridge Vibrations', Proceedings of the IEEE International conference on Green Energy and Applications (ICGEA), pp. 134-137.
- [23] Tsukamoto, T, Umino, Y, Shiomi, S, Yamada, K & Suzuki,
  - a. 2018, 'Bimorph Piezoelectric Vibration Energy Harvester with Flexible 3D Meshed-Core Structure for

Low Frequency Vibration', Science And Technology Of Advanced Materials, vol. 19, no. 1, pp. 660–668.

[24] Dong, X, Yi, Z, Kon, L, Tia, Y, Liu, J & Yang, B 2019,

'Design, Fabrication, and Characterization of Bimorph Micromachined Harvester with Asymmetrical PZT Films', Journal of Microelectromechanical Systems, vol. 28, no. 4, pp. 700–706.

[25] Yang, K, Zheng, JC, John, D, Jim, S & Meiling, Z 2021,
'Strongly Coupled Piezoelectric Energy

Harvesters: Optimised Design with Over 100 mW Power, High Durability and Robustness for Self-Powered Condition

Monitoring', Energy Conversion and Management, vol. 237, pp. 1-14.

[26] D. Chaudhuri, S. Kundu, and N. Chattoraj, "Design and analysis of MEMS based piezoelectric energy harvester for machine monitoring application," Microsystem Technologies, vol. 25, no. 4, pp. 1437–1446, 2019.
[Online]. Available:

https://doi.org/10.1007/s00542-018-4156-z

[27] R. Sriramdas, S. Chiplunkar, R. M. Cuduvally, and R.

INTERNATIONAL JOURNAL OF SCIENTIFIC RESEARCH IN ENGINEERING AND MANAGEMENT (IJSREM)VOLUME: 08 ISSUE: 07 | JULY - 2024SJIF RATING: 8.448ISSN: 2582-3930

Pratap, "Performance enhancement of piezoelectric energy harvesters using multilayer and multistep beam configurations," IEEE Sensors Journal, vol. 15, no. 6, pp. 3338–3348, 2015.

- [28] S. Paquin and Y. St-Amant, "Improving the performance of a piezoelectric energy harvester using a variable thickness beam," Smart Materials and Structures, vol. 19, no. 10, p. 105020, 2010.
- [29] D. S. Ibrahim, S. Beibei, O. A. Oluseyi, and U. Sharif, "Performance analysis of width and thickness tapered geometries on electrical power harvested from a unimorph piezoelectric cantilever beam," in 2020 IEEE 3rd International Conference on Electronics Technology (ICET). IEEE, 2020, pp. 100–104.
- [30] J. Zhang, X. Xie, G. Song, G. Du, and D. Liu, "A study on a near-shore cantilevered sea wave energy harvester with a variable cross section," Energy Science & Engineering, vol. 7, no. 6, pp. 3174–3185, 2019.
- [31] S. Kundu and H. B. Nemade, "Piezoelectric vibration energy harvester with tapered substrate thickness for uniform stress," Microsystem Technologies, vol. 27, no. 1, pp. 105–113, 2021.
- [32] Mangla, C, Ahmad, M & Uddin, M 2018, 'Genetic Algorithm Based Optimization for System of Nonlinear Equations', International Journal of Advanced Technology and Engineering Exploration, vol. 5, pp. 2394-7454.
- [33] Ye, G, Yan, J, Wong, ZJ, Soga, K & Seshia, A 2009,
  'Optimization of a Piezoelectric System for Energy Harvesting from Traffic Vibrations', IEEE-ULTSYM, pp. 759-762.
- [34] Rahman, CM, Rashid, TA 2021, 'A New Evolutionary Algorithm: Learner Performance Based Behavior Algorithm, Egyptian Informatics Journal, vol. 22, no. 2, pp. 213-223.
- [35] Raj, PVR & Santhosh, B 2019, 'Parametric Study and Optimization of Linear and Nonlinear Vibration Absorbers

Combined with Piezoelectric Energy Harvester', International Journal of Mechanical Science, vol. 152, pp. 268-279.

[36] Tawhid, MA & Ahmed, FA 2017, 'A Hybrid Grey Wolf Optimizer and Genetic Algorithm for Minimizing Potential Energy Function', Memetic Computing, vol. 9, pp. 347359.