

# Oxide ion polarizability, Optical basicity, Bond strength, Nonlinear susceptibility of glass systems (Review)

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**Abstract** – A review of an interpretation of optical properties of oxides and oxide glasses in terms of the electronic ion polarizability and average single bond strength, given by V. Dimitrov and T. Komatsu.

Here a review is taken in glass systems in terms of refractive index, optical band gap, oxide ion polarizabilities, optical basicities, average single bond strength and Third-order nonlinear optical susceptibilities.

*Key Words*: Refractive index, optical bang gap, oxide ion, polarizability, optical basicity, average single bond strength, third-order nonlinear optical susceptibility

### **1. INTRODUCTION**

The estimation of free ion electronic polarizability of ions is a subject of so-called polarizability approach in material science, which is well known especially in the field of glass science as done by Pauling <sup>[1]</sup>, Born and Heisenberg <sup>[2]</sup>, Fajans and Joos <sup>[3]</sup>, J. Mayer and M. Mayer <sup>[4]</sup>, Kordes <sup>[5]</sup> and

Estimation of polarizability would be useful especially with respect to oxide crystals and glasses, which are of technological importance as optical and electronic materials. The most familiar and widely used relationship in this approach is Lorentz-Lorenz equation.

Duffy and Ingram<sup>[6,7]</sup> proposed Optical basicity properties of the oxides and glasses related to the polarization of oxide ions in the material matrix and represents their ability to transfer electron density to surrounding cations.

Dimitrov and Komatsu<sup>[8,9]</sup> have shown a good agreement between theoretical optical basicity ( $\Lambda_{th}$ ) and refractive index based optical basicity  $\Lambda(n)$  for large number of binary oxide glasses, including phosphate, borate, silicate, germanate, tellurate and titanate. The optical basicity can be experimentally determined but the applicability of the method is rather limited. Hence it is desirable to derive the values for many oxides on the basis of the similarity in the physical nature of the polarizability and the optical basicity.

Honma et al. <sup>[10-11]</sup> studied the refractive index based optical band gap, oxide ion polarizabilities and optical basicities.

Terashima <sup>[12-13]</sup> study on average single bond strength and Third-order nonlinear optical susceptibility in binary glasses and more recently Dimitro and Komatsu <sup>[14]</sup> have established the correlation existing between third order nonlinear susceptibility  $\chi^{(3)}$ , average single bond strength B<sub>M-O</sub>, optical basicity and oxide ion polarizability with high refractive index basic alkali and alkaline earth glasses.

## 2. THEORY

Dimitrov and Sakka <sup>[15</sup> have determined the optical basicity for numerous single oxides on the basis of their refractive index  $\Lambda(n_o)$  and Energy gap  $\Lambda(E_g)$  by using equations,

$$\alpha_{o2-} (n_o) = [(V_m/2.52) (n_o^2-1) / (n_o^2+2) - p\alpha_i] (q)^{-1}$$
(1)

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$$\alpha_{o2}(E_g) = [(V_m/2.52) (1 - (E_g/20)^{1/2}) - p\alpha_i] (q)^{-1}$$
(2)

In above equations  $V_m$  is molar volume,  $n_o$  is refractive index, p & q are cations and oxide ions in the chemical formula of oxide  $A_pO_q$ ,  $\alpha_i$  is cation polarizability,  $E_g$  is energy gap, and  $\alpha_{o2}$  polarizability of the oxide ion.

$$\Lambda = 1.67[1 - (1/\alpha_{o2})]$$
(3)

Honma et.al.<sup>[10,11]</sup> have applied above equations (2) to calculate the electronic oxide ion polarizability  $\alpha_{o2}$ -(E<sub>o</sub>) and refractive index based  $\alpha_{o2}$ -(n<sub>o</sub>) for Sb<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> and Bi<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> glasses using experimental data for optical band gap E<sub>o</sub>. Similarly by using equation (3) the optical basicity of Sb<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> and Bi<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> glasses are calculate using the experimental data for optical band gap E<sub>o</sub> are listed in Tale 1. It was observed that there is general tendency of increase oxide ion polarizability with increasing refractive index and decreasing energy gap.

The average single bond strength of oxide glasses have been determined by Terashima et, al.<sup>[12,13]</sup> using following equations,

For Bi<sub>2</sub>O-B<sub>2</sub>O<sub>3</sub> glasses

$$B_{M-O} = x B_{Bi-O}^{(6)} + (1-x)[N_3 B_{B-O}^{(3)} + N_4 B_{B-O}^{(4)}$$
(4)

For Sbi<sub>2</sub>O-B<sub>2</sub>O<sub>3</sub> glasses

$$B_{M-O} = x B_{Sb-O}^{(3)} + (1-x)[N_3B_{B-O}^{(3)} + N_4B_{B-O}^{(4)}$$
 (5)

where  $N_3$  and  $N_4$  are mol fraction of  $BO_3$  and  $BO_4 {\rm groups}$  in one molecule of glass and  $B_{B \cdot O} \,^{(3)}$  and  $B_{B \cdot O} \,^{(4)}$  are the single bond strength of B-O bonds in the BO\_3 and BO\_4 groups , respectively.  $B_{Bi \cdot O} ^{(6)}$  and  $B_{Sb \cdot O} ^{(3)}$  are the single bond strength of Bi-O and Sb-O bonds in BiO\_6 and SbO\_3 groups , respectively.

Third-order nonlinear optical susceptibility is calculated by using equations,

$$\chi^{(3)} = (1.4*10^{-11}) / [(E_{opt}-1.96)(E_{opt}-1.31)(E_{opt}-0.65)]$$
(6)  
$$\chi^{(3)} = \{ [(n_o^2 - 1)/4\pi]^4 * 10^{-10} \text{ esu.}$$
(7)

Where  $n_o =$  linear refractive index.

The purpose of the article is to consider the status of oxide ion polarizability and optical basicity approach in the glass systems and to emphasize the role of the optical band gap, which helpful to the new researchers.



## **3. RESULT AND DISCUSSION**

**3.1 Refractive index and optical band gap:** In this review the refractive index and optical band gap in  $Sb_2O_3$ - $B_2O_3$  systems and  $Bi_2O_3$ - $B_2O_3$  systems studied by Honma et.al, are taken,



Fig. 3.1.(a) Variation of no & Eo(eV) of Sb2O3-B2O3 system.

Figure 3.1.(a) shows that the refractive index ( $n_o$ ) increasing form 1.474–1.881 optical energy gap  $E_o(eV)$  decreases from 4.51–3.62 (eV). It was observed that there is general tendency of increasing refractive index with decreasing energy gap.



Fig. 3.1.(b) Variation of  $n_o \& E_o(eV)$  of  $Bi_2O_3$ - $B_2O_3$  systems.

Figure 3.1.(b) shows that the refractive index increasing form1.818–2.129, optical energy gap decreases from  $3.65-3.03 \text{ E}_{0}(\text{eV})$ . It was observed that there is general tendency of increasing refractive index with decreasing energy gap.

**3.2 Oxide ion polarizability and Optical basicity:** In this review the refractive index based electronic oxide ion polarizability  $\alpha_{o2}$ - $(n_o)$ ,  $\alpha_{o2}$ - $(E_o)$  and optical basicity  $\Lambda(n_o)$ ,  $\Lambda(E_o)$  in Sb<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> and Bi<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> glasses studied by Honma et.al, are taken on four axis graph,



Fig. 3.2(a) plot of  $\alpha o_2$ -(n<sub>o</sub>),  $\alpha o_2$ -(E<sub>o</sub>);  $\Lambda(n_o)$ ,  $\Lambda(E_o)$  of Sb<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> systems

Figure 3.2 (a) shows that the refractive index based oxide ion polarizability in Sb<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> systems  $\alpha_{o2}$ -(n<sub>o</sub>) increasing form1.331–2.417 and  $\alpha_{o2}$ -(E<sub>o</sub>) also increases from 1.995-3.159; Optical basicity  $\Lambda(n_o)$  increases from 0.415-0.979 and  $\Lambda(E_o)$  increases from 0.833-1.141. It is general tendency of increasing oxide ion polarizability and optical basicity.

#### Table 1:

System	Mol % of first oxide	n <sub>o</sub>	Eo (eV)	α <sub>o2</sub> . (n <sub>o</sub> )	α <sub>o2-</sub> (E <sub>o</sub> )	$\Lambda(n_o)$	Λ(E₀)
$Sb_2O_3$ - $B_2O_3$	0	1.446	7.20	1.331	1.995	0.415	0.833
	10	1.474	4.51	1.365	2.614	0.447	1.031
	20	1.570	4.26	1.570	2.670	0.606	1.045
	30	1.707	4.12	1.877	2.720	0.78	1.056
	40	1.767	3.95	2.010	2.794	0.839	1.072
	50	1.820	3.89	2.153	2.867	0.894	1.088
	60	1.853	3.72	2.317	3.059	0.949	1.124
	70	1.881	3.62	2.417	3.159	0.979	1.141
Bi <sub>2</sub> O <sub>3</sub> - B <sub>2</sub> O <sub>3</sub>	25	1.818	3.65	1.48	2.03	0.542	0.847
	30	1.836	3.55	1.626	2.224	0.643	0.919
	40	1.976	3.32	1.97	2.452	0.822	0.989
	50	2.074	3.2	2.171	2.557	0.901	1.017
	60	2.097	3.06	2.284	2.704	0.939	1.052
	65	2.129	3.03	2.37	2.759	0.965	1.065

Table 1 Refractive index  $n_o$ , optical band gap  $E_o$ , oxide ion polarizabilities  $\alpha_{o2-}$ ( $n_o$ ),  $\alpha_{o2-}(E_o)$ , optical basicity  $\Lambda(n_o)$  and  $\Lambda(E_o)$  of Sb<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> and Bi<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> glasses.



Fig. 3.2.(b) plot of  $\alpha o2$ -(n<sub>o</sub>),  $\alpha o2$ -(E<sub>o</sub>);  $\Lambda(n_o)$ ,  $\Lambda(E_o)$  of Bi<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> systems

Figure 3.2 (b) It shows that the refractive index based oxide ion polarizability in Bi<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> systems  $\alpha_{o2}$ -(n<sub>o</sub>) increasing form1.48–2.37 and  $\alpha_{o2}$ -(E<sub>o</sub>) also increases from 2.03-3.2.759; Optical basicity  $\Lambda$ (n<sub>o</sub>) increases from 0.542-0.965 and  $\Lambda$ (E<sub>o</sub>) increases from 0.847-1.065. It is general tendency of increasing oxide ion polarizability and optical basicity.

# **3.3** Bond strength and third order nonlinear optical - susceptibility:

Single bond strength BM-0 introduced by Sun in fact represents the single bond energy of an averaged M-O chemical bond in the oxide expressed by its dissociation energy; later on equations for calculation of average single bond strength BM-0



in glasses have been derived taking into account the contribution of different structural units.



Fig. 3.3.(a) R.I.( $n_o$ ),  $B_{M-O}$  kJ/mol,  $\chi^{(3)}$  10<sup>-14</sup> eus.of Sb<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> systems

Figure 3.3 (a), shows that the refractive index based values of average single bond strength  $B_{M\text{-}O}$  decreases from 469-308 kJ/mol, and third order nonlinear susceptibility  $\chi^{(3)}$  increases from 4.96-51.5x10<sup>-14</sup>esu., in Sb<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> systems It is general tendency of increasing third order nonlinear susceptibility and decreasing of average single bond strength.



Fig. 3.3.(b) R.I.( $n_o$ ),  $B_{M-O}$  kJ/mol,  $\chi^{(3)}$  10<sup>-14</sup> esu., of  $Bi_2O_3$ -B<sub>2</sub>O<sub>3</sub> systems

Figure 3.3 (b) It shows that the refractive index based values of average single bond strength  $B_{M-O}$  decreases from 361-233 kJ/mol, and third order nonlinear susceptibility  $\chi^{(3)}$  increases from 31.9-118x10<sup>-14</sup>esu., in Bi<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> systems It is general tendency of increasing third order nonlinear susceptibility  $\chi^{(3)}$ , and decreasing average single bond strength  $B_{M-O}$ .

### 3.4 Bond strength and third order nonlinear optical susceptibility in alkali and alkaline earth glasses:

Dimitro and Komatsu  $^{[12]}$  have established the correlation existing between third order nonlinear susceptibility  $\chi^{(3)}$ , average single bond strength  $B_{M\text{-}O}$ , optical basicity and oxide ion polarizability with high refractive index basic alkali and alkaline earth glasses.



Fig. 3.4.(a) R.I.( $n_0$ ),  $\alpha o2$ -(no),  $\Lambda(no)$  of Na<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> systems

Figure 3.4(a) shows that the refractive index increases from 1.481-1.517, oxide ion polarizability  $\alpha_{o2}$ -(n<sub>o</sub>) increases from 1.31-1.417 and optical basicity  $\Lambda(n_o)$  also increases from 0.452-0.493 in Na<sub>2</sub>O-B<sub>2</sub>O<sub>3</sub> systems. It is general tendency of increasing oxide ion polarizability and optical basicity.



Fig. 3.4.(b) R.I.( $n_0$ ),  $\alpha o2$ -(no),  $\Lambda(no)$  of Na<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub> systems.

Figure 3.4(b) shows that the refractive index increases from 1.482-1.506, oxide ion polarizability  $\alpha_{o2}$ -(n<sub>o</sub>) increases from 1.54-1.648 and optical basicity  $\Lambda(n_o)$  also increases from 0.586-0.656 in Na<sub>2</sub>O-SiO<sub>2</sub> systems. It is general tendency of increasing oxide ion polarizability and optical basicity.



Fig. 3.4.(c) R.I.(n\_o),  $B_{M \cdot O} \, kJ/mol, \, \chi^{(3)} \, 10^{-14}$  esu., of  $Na_2O\text{-}SiO_2$  systems.

Figure 3.4 (c) It shows that the refractive index based values of average single bond strength  $B_{M-O}$  decreases from 389-324 kJ/mol, and third order nonlinear susceptibility  $\chi^{(3)}$  increases from 3.5-4.9x10<sup>-14</sup>esu., in Na<sub>2</sub>O-SiO<sub>2</sub> systems It is general tendency of increasing oxide ion polarizability and optical basicity.



Fig. 3.4.(d) R.I.(n\_o),  $B_{M \cdot O} \, kJ/mol, \, \chi^{(3)} \, 10^{-14}$  esu., of PbO-SiO\_2 systems.



Figure 3.4 (d) It shows that the refractive index based values of average single bond strength  $B_{M-O}$  decreases from 356-247 kJ/mol, and third order nonlinear susceptibility  $\chi^{(3)}$  increases from 7.1-31.1x10<sup>-14</sup>esu., in PbO-SiO<sub>2</sub> systems It is general tendency of increasing third order nonlinear susceptibility  $\chi^{(3)}$  decreasing average single bond strength  $B_{M-O}$ .

### Table 2:

System	Mol % of first oxide	n <sub>o</sub>	α <sub>o2-</sub> (n <sub>o</sub> )	$\Lambda(n_o)$	B <sub>M-O</sub> kJ/mol	$\chi^{(3)}_{10^{-14}}$ esu
$Na_2O-B_2O_3$	5.12	1.481	1.371	0.452	477	
	10.33	1.491	1.37	0.451	455	
	15.2	1.497	1.371	0.452	435	
	20.23	1.502	1.374	0.454	414	
	25.13	1.509	1.38	0.46	394	
	29.85	1.516	1.392	0.471	374	
	34.2	1.517	1.417	0.493	356	
Na <sub>2</sub> O- SiO <sub>2</sub>	15	1.482	1.54	0.586	389	3.5
	20	1.49	1.565	0.603	372	3.8
	25	1.498	1.591	0.621	354	4.3
	30	1.504	1.627	0.643	336	4.7
	33	1.506	1.648	0.656	324	4.9
PbO- SiO <sub>2</sub>	30	1.749	1.442	0.513	356	7.1
	40	1.811	1.516	0.568	326	12.7
	50	1.859	1.608	0.631	297	18.1
	60	1.942	1.65	0.658	268	23
	67	1.996	1.74	0.71	247	31.1

Table 2 Refractive index  $n_o$ , oxide ion polarizabilities  $\alpha_{o2}.(n_o)$ , optical basicity  $\Lambda(n_o)~B_{M\cdot O}~kJ/mol$  and  $\chi^{(3)}~10^{-14}$  esu of  $Na_2O-B_2O_3$  and  $Na_2O-SiO_2$ , PbO-SiO\_2 glass systems.



Fig. 3.4.(e) R.I.(n<sub>o</sub>), αo2-(no), Λ(no) of PbO-SiO<sub>2</sub> systems

Figure 3.4(e) shows that the refractive index increases from 1.749-1.996, oxide ion polarizability  $\alpha_{o2}$ -(n<sub>o</sub>) increases from 1.442-1.740 and optical basicity  $\Lambda(n_o)$  also increases from 0.513-0.710 in PbO-SiO<sub>2</sub> systems. It is general tendency of increasing oxide ion polarizability and optical basicity.

### CONCLUSION

The polarizability increases with increasing Sb<sub>2</sub>O<sub>3</sub> and Bi<sub>2</sub>O<sub>3</sub> content, but the values of oxide ion polarizabilities  $\alpha_{o2}$ .(E<sub>o</sub>) and the values of optical basicity  $\Lambda(E_o)$  are larger than those obtained for oxide ion polarizabilities  $\alpha_{o2}$ .(n<sub>o</sub>) and optical basicity  $\Lambda(n_o)$ .Consequently it seems to be more informative to use oxide ion polarizabilities  $\alpha_{o2}$ .(n<sub>o</sub>) and optical basicity  $\Lambda(n_o)$  for the analysis of the electronic polarizability of these glass. It has been concluded that high refractive index basic glasses with increased tendency in oxide ion polarizabilities  $\alpha_{o2}$ .(n<sub>o</sub>),  $\alpha_{o2}$ .(E<sub>o</sub>) and in optical basicity  $\Lambda(n_o)$ ,  $\Lambda(E_o)$ ; and decreasing average single bond strength B<sub>M-O</sub> with increasing the third order nonlinear optical susceptibility  $\chi^{(3)}$ .

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