

# Runoff Characteristics based on Geo-morphological Instantaneous Unit Hydrograph over Humid Region of Himalayas of Bhutan

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**Abstract** It is critical to quantify runoff that would be generated due to rainfall in a catchment which would in turn help in predicting the nature of response from a catchment that can be used to come up with a strategic planning and implementation to prevent from certain foreseen or unforeseen calamities. Most of the sub-catchments in Bhutan are un-gauged, which results in the insufficient hydrological data for validating the accuracy of any hydrological model. The current study is approached with identification of reliable hydrological model with the help of real data obtained through customized gauging stations developed using Arduino chip that works on batteries, using sonar sensors. To overcome the issue of insufficient data sets, Om chu river, situated at Phuentsholing is chosen to be gauged for the study. This practical approach towards the analysis of intensity and response of catchment, would help engineers to foresee the possible calamities if any and design the structures accordingly with the reasonable costing.

**Key Words:** quantify, runoff, catchment response, ungauged, hydrological models, arduino

## 1. INTRODUCTION (Size 11, Times New roman)

Water is the most important resource of Himalayan countries like Bhutan as hydro power is one of the major sources of revenue. On the other hand, it can also be the major cause of problems prevailing in the country especially during monsoon. According to UNDP, Bhutan's climatic conditions vary considerably from one region to another owing to mountainous topography that influences every sphere of the environment due to drastic difference in altitude. The country can be divided into three climatic zones based on annual rainfall namely the Southern Himalayas experiencing heavy rainfall, the central belt with moderate rainfall and high Himalayas with less rainfall. The rainfall in the country is attributed to Indian monsoon that begins by early June and lasts till end of October. During the rainy season, the southern region of the country, often witnesses calamities like damages to infrastructures such as bridges and river training structures, because of the considerable flow.

To counteract these problems, it is critical to quantify runoff that would be generated due to rainfall in a catchment. Further, this can be helpful to manage runoff adequately thereby predicting the nature of response from a catchment which would in turn, can be used to come up with a strategic

planning and implementation to prevent from certain predicted calamities.

There are many tools that were devised to predict the catchment response of which only few of these models are applicable in catchments of Bhutan. It is mainly due to unavailability of past hydrological datasets. Through the knowledge and understanding of the catchment environment, a new method named Geomorphological Instantaneous Unit Hydrograph (GIUH) have gained popularity among the hydrologists to estimate runoff. This method employs catchment geomorphological parameters to estimate runoff thus, it is applicable even for un-gauged basins such as Om Chu Basin.

In this study, GIUH based Nash and Clerk model along with Snyder synthetic unit hydrograph method and central water commission method (CWC) has been applied. The methods have been reasonable to predict the catchment response in catchment in India. The accuracy of the models in Bhutan's geography is checked and validated through the study to come up with most reasonable models for runoff quantification in Bhutan's river basin.

The study aims to come up with a hydrological model that gives a hydrograph of ungauged catchment in Bhutan. The GIUH produces output in instantaneous unit hydrograph (IUH). IUH is converted to unit hydrograph (UH). Finally, hydrograph is obtained from the UH using the effective rainfall intensity data.

## 2. DEVELOPMENT OF GUIH MODELS

The development of GIUH based clerk and Nash model includes the extraction of the catchment geomorphological characteristics, estimation of the parameters. Procedure to develop GIUH models are mentioned below.

### 2.1. GIUH based Clerk model

Clerk instantaneous unit hydrograph (IUH) due to instantaneous rainfall excess is based on a concept that the catchment acts like a linear channel. Parameters of the Clerk IUH are time of concentration ( $T_c$ ) and the storage coefficient ( $R$ ) expressed in hour. GIUH based Clark model

has two parameters, time of concentration ( $T_c$ ) and catchment storage coefficient ( $R$ ). These parameter estimation are explained in detail in (Timothy D. Straub, Charles S. Melching, 2000). In brief,

$$T_c = 1.54L^{0.875}S^{-0.181} \text{ (h)} \quad (1)$$

$$R = 16.4L^{0.342}S^{-0.79} \text{ (h)} \quad (2)$$

Determination of time area diagram is a mandatory for development of Clark model. Clark based IUH can be obtained using the following equation

$$U_i = 2C_1L_i + C_2U_{i-1} \quad (3)$$

Where  $U_i$  is  $i$  th ordinate of the IUH,  $C_1 = 2\Delta t R + 0.5\Delta t$  and  $C_2 = R - 0.5\Delta t R + 0.5\Delta t$   $\Delta t$  is computational interval.  $L_i$  is inflow rate between an inter-isochronal areas.

## 2.2. GIUH based Nash model

The instantaneous unit hydrograph from Nash model was developed on a conceptual consideration that the catchment response can be linked through a linearly arranged reservoir in series that act as a cascade. Parameter of the Nash model are the number of  $n$  linear reservoir ( $n$ ) and the storage coefficient ( $k$ ). It is explained in detail in (Kumar, Chatterjee, Singh, Lohansi, & Kumar, 2007). It is calculated using the following equation

$$n = 3.29 \left( \frac{R_B}{R_A} \right)^{0.78} R_L^{0.05} \quad (4)$$

$$k = \frac{0.44L_n}{V} \left( \frac{R_B}{R_A} \right)^{0.55} R_L^{-0.38} \frac{1}{(n-1)} \quad (5)$$

Where  $n$  and  $k$  are Nash parameter,  $R_A$ ,  $R_B$  and  $R_L$  are the Horton ratio. The IUH by the GIUH based Nash model is obtained by the following equation,

$$Q(t) = 1$$

$$Q(t) = \frac{1}{k \Gamma_n} \left( \frac{t}{k} \right)^{n-1} e^{-\frac{t}{k}} \quad (6)$$

Where,  $Q(t)$  = IUH ordinate (per hour),  $t$  is time interval of the sample taken (hour),  $n$  and  $k$  are the Nash parameter.

## 2.3. Evaluation of the computed storm hydrograph with the observed storm hydrograph

Since the evaluation of two hydrograph deals with the checking in the variation of each ordinate of hydrograph, objective function have been applied for evaluation of observed and computed storm hydrograph by each model. The function includes (I) Efficiency (EFF), (II) Absolute

average error (AAE) and (III) Root mean square error (RMSE).

$$EFF = \frac{\sum_{i=1}^n (Q_{oi} - Q)^2 - \sum_{i=1}^n (Q_{oi} - Q_{ci})^2}{\sum_{i=1}^n (Q_{oi} - Q)^2} * 100 \quad (7)$$

$$AAE = (Q_{oi} - Q_{ci})n \quad (8)$$

Where  $n$  is number of ordinates.

$$RMSE = \sqrt{\frac{\sum (Q_{oi} - Q_{ci})^2}{n}} \quad (9)$$

## 3. STUDY AREA

The Om Chu is a perennial river originating from the slope of Sorchen area near Gedu and flows through Phuentsholing town, Bhutan. For the current study, the catchment outlet is specifically chosen at 26°52'05.9" N latitude and 89°23'50.6" E longitude. The drainage area is about 18.06 km<sup>2</sup> with the varying elevation between 264m to 1420m above the sea level. The longitudinal slope of the catchment is 0.179m/m with longest river of length 7.024 km. The catchment area falls under the moist temperate zone and receives about 4383mm of average annual rainfall. The maximum precipitation is observed within the month of July and October (NCHM).

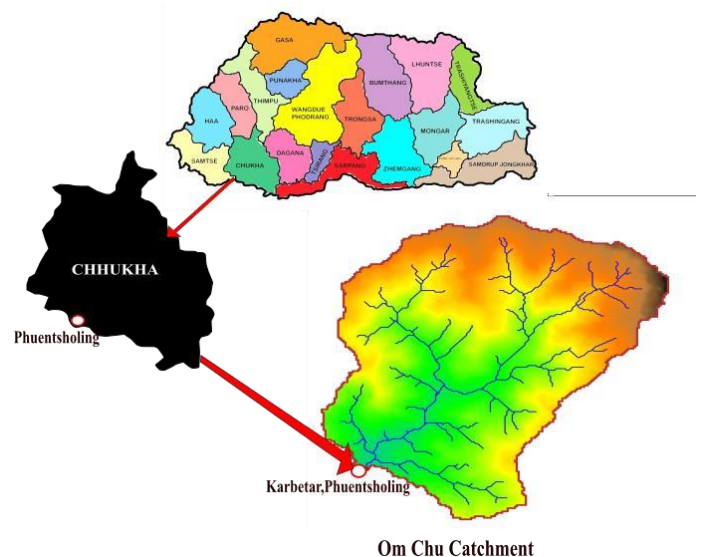
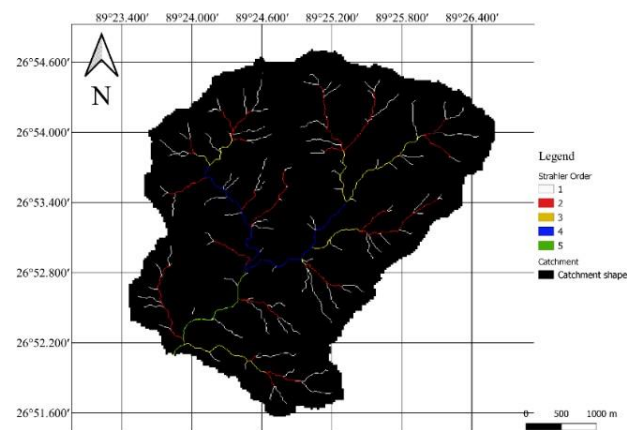


Figure 1 Om Chu river catchmen

## 1. EXTRACTION OF CATCHMENT GEOMORPHOLOGICAL CHARACTERISTICS THROUGH GIS AND DEM

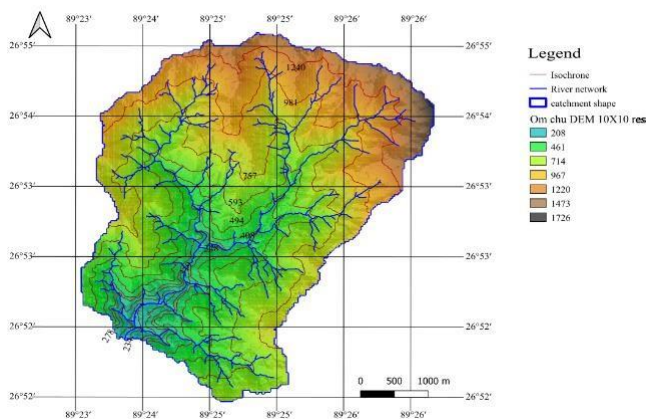
GIUH method involves the use of the use of distinct catchment characteristics such as the catchment area, perimeter, slope of the catchment and the length of the river channel in flowing through the catchment. Surveying these data in the field is a tedious and labor-intensive work. Alternative method includes the use of topo map and the use of GIS. QGIS tool are free and a powerful tool that have sufficient tool to work with to determine all the parameter required for the development of GIUH models.



**Figure 3** Stream order by Strahler stream order method.

**Table 2** Detail of stream segment of Om Chu river

stream order (U)	No. (N <sub>U</sub> )	Stream Length (Km)	Mean Stream Length (Km)	Mean Stream Area (Km <sup>2</sup> )
1	108	24.96	0.23	0.08
2	21	11.71	0.23	0.39
3	6	6.32	0.18	1.78
4	2	3.81	0.24	6.77
5	1	2.1	0.14	18.81



**Figure 2** Drainage map of Om chu river, Bhutan

**Table 1** Catchment characteristics

Sl. No.	Geographical parameter	Symbol	Magnitude
1	Area (sq. km)	A	18.08
2	Perimeter (km)	P	24.69
3	Basin length (km)	L <sub>b</sub>	5.9
4	Longitudinal slope	S	0.179 m/m
5	Channel stream order	O	5
6	Length of outlet from centroid of the catchment	L <sub>c</sub>	3.57
7	Longest length of stream	L	7.024 km

Om chu river network has been shown in the figure 1. Strahler's method of stream order is applied in Om Chu and river has highest order 5. Using stream order data and table 1 data, RA, RB and RL are 4.429, 1.924 and 1.882 respectively. Using the Aster DEM, geomorphological characteristics of the Om Chu has been obtained in progressive manner.

## 5. DEVELOPMENT OF HYDROGRAPH FROM COMPUTED IUH

A significant step for the validation and application of any hydrological methods involves the generation of the hydrograph from the model. For GIUH models, the final output is an IUH. It is converted to UH by taking the average of the IUH data with another same IUH data lagged by an hour to obtain 1D hour UH. To convert UH to H, the term effective rainfall and base flow comes in picture. Phi index for the Om chu river is obtained through experimental method where the infiltration of the soil in the catchment is determined and taken as the average which is the phi index of the catchment. For Om chu river it is 1.24 cm/h. Effective rainfall is the difference of the rainfall intensity and the phi index. To obtain the hydrograph, the excess rainfall intensity is multiplied to the UH ordinate to obtain the hydrograph.

### 5.1. Collection of the storm hydrograph from the field

Validation of the hydrological model requires an observed field data. For an ungauged data, obtaining field data mean to gauge the river at the catchment outlet. For Om chu river, since the catchment response to a rainfall is abrupt, manual recording prove to be hard and risky. Also, lack of any device to measure the velocity of the river made it harder. In this scenario, development of the data logger to collect the stage hydrograph and application of noncontact discharge measurement technique come in action. Chezy's method for discharge measurement for a small catchment produces a very high discharge, which is not accurate (Tazioli, 2011). An equation to compute discharge with only stage data. Simplifying the working by removing the need for measurement of the velocity. The method showed accuracy of 99% on a hypothetical test. Reasonable rating curve was obtained for the Chattahoochee river, USA (Perumal & Adhikari, 2019). The equation is known as Approximate ConvectionDiffusion wave equation given by

$$Q_2 - \frac{Q_0^2}{2S_0 T_2 C_2^2 \Delta t} + \frac{\frac{1}{2} \sqrt{\left( \frac{Q_0^2}{S_0 T_2 C_2^2 \Delta t} \right)^2 + 4(Q_0^2 + \frac{2Q_0^2 Q_1}{S_0 T_2 C_2^2} + \frac{2Q_0^2}{S_0 T_2 C_2^2} \left[ \frac{A_2 - A_1}{\Delta t} \right])}}{2} \quad (9)$$

Where, T is top width, c is celerity, So is channel bed slope, Q1 is discharge at previous time step and Q0 is steady discharge. For Om Chu river, for a steady flow of by ACDW method, discharge obtained was to be fairly close to discharge obtained by Manning's formula.

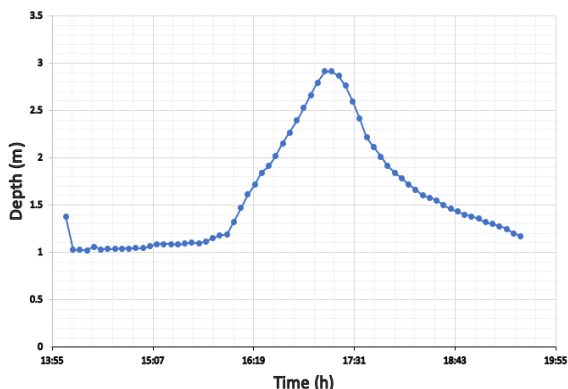


Figure 4 Stage hydrograph

## 2. RESULT AND ANALYSIS

For computation of the GIUH based Clerk model, inflow rate corresponding to each time area diagram was computed. Using the parameter and the inflow rate, ordinate of the IUH was obtained. For GIUH based Nash model is much simpler and uses the parameter and the computational time for the generation of the IUH. The IUH by GIUH based and GIUH based Nash model is shown below.

### GIUH based Clark model-IUH

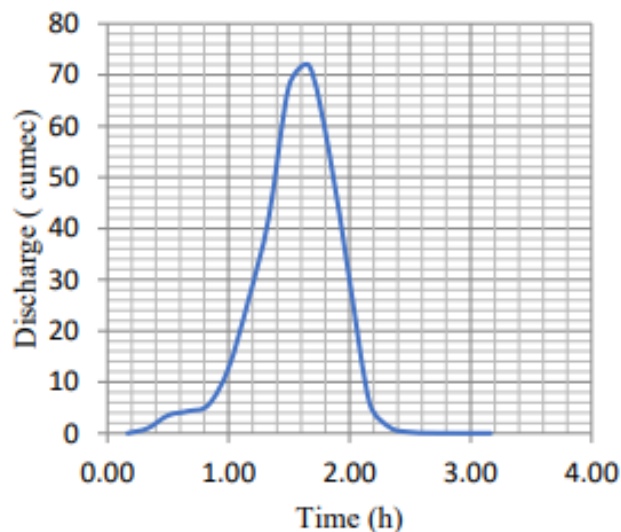


Figure 6 IUH by Clark model

### GIUH based Nash model-IUH

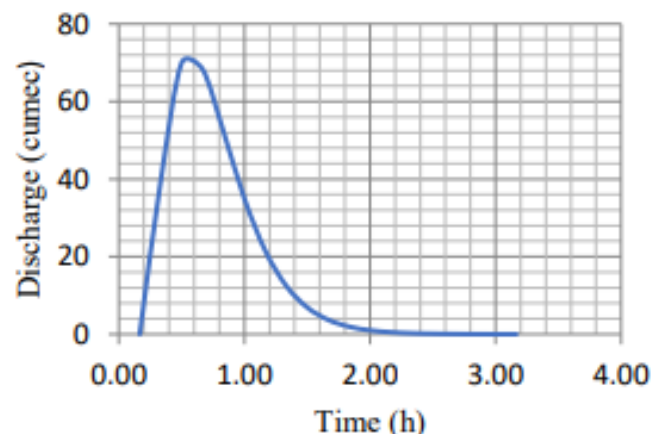
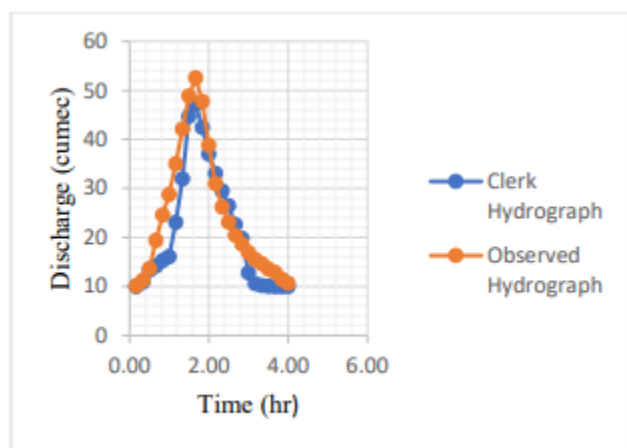


Figure 7: IUH by Nash model

For the validation of the work, the IUH is used to computed the storm hydrograph for the Om chu for a rainfall event with rainfall intensity of 22mm/h. Phi index for the catchment is 12.36mm/h. Base flow of the catchment was about 10 cumec. The result by both the method is displayed below.

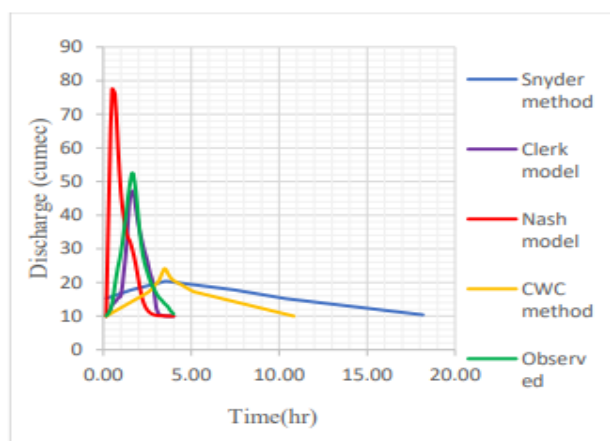




**Figure 9** Nash based hydrograph vs observed hydrograph

**Table 4** Magnitude of objective function for Nash model

Objective function	EFF	AAE	RMSE
Magnitude	-213.5	0	22.97



**Figure 9** Comparison of Clark, Nash based hydrograph with observed hydrograph

This is being clear in the figure 9, that the catchment response for this particular event is shown better by GIUH based Clerk model. GIUH based Nash model is found to give the reasonable rainfall event duration but giving an early peak than expected. Empirical method of determining unit hydrograph is simple and easy to carry out the parameter estimation but the for Om Chu river, the result is not reasonable both in peak discharge as well as the duration of catchment response.

### 3. CONCLUSIONS

Geomorphological IUH based hydrological models mainly uses geomorphologic parameters to construct IUH. GIUH is easy and cost effective because the geomorphological parameters can be easily obtained using QGIS and DEM. In addition to that, it doesn't require past hydrological rainfall runoff data and this particular reason makes hydrologist to prefer this method over conventional method. Based on the comparison between observed hydrograph obtained from field and the hydrograph through different hydrological models, it is concluded that geomorphological IUH can be applied in the Bhutan's river basin. Comparing the peak discharge, time of concentration and time to peak with field hydrograph, Clark model is displayed the reasonable accuracy for the Om chu river basin for an event

Furthermore, GIUH models showed the good catchment response however empirical model's response was slight less than field hydrograph.

### ACKNOWLEDGEMENT

The heading should be treated as a 3<sup>rd</sup> level heading and should not be assigned a number.

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